

## Surrogate Models to Cope With Users' Behaviour in School Building Energy Performance Calculation

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### Abstract

The paper investigates the use of surrogate models for probabilistic building performance simulation that can be used for multiple applications across life cycle phases. The workflow presented aims to highlight a possible continuity among design and operation phase practices, in order to contribute to the reduction of the gap between simulated and measured performance, considering in particular the uncertainties caused by users' behaviour. Design phase simulation work is generally affected by relevant temporal and economic constraints and, consequently, a successful approach should enhance current design practices and implement new features which have to be automated, to decrease additional modelling effort. The parametric data obtained in the initial design phase by means of a detailed model are used to train an Artificial Neural Network model. The results obtained by this model are compared with the ones obtained with a Resistance-Capacitance model. The approach is automated and tested for robustness using Monte Carlo simulation technique. This technique is used to identify, already in the design phase, probabilistic performance boundaries. The case study chosen is the eLUX Lab building at the Smart Campus of University of Brescia, in which highly variable occupancy patterns are present.

### Introduction

The European Commission established a long-term objective of decreasing the CO<sub>2</sub>-emission levels for the building sector by 88-91% in 2050, compared to 1990 levels (COM, 2011). This target represents also a prerequisite for meeting other EU economic and climate goals and energy performance in the whole life cycle of buildings becomes a relevant matter in terms of sustainability and resource efficiency at the EU level. Actual energy performance often differs from predicted one due to simplifications and approximations normally associated with modelling approaches (De Angelis et al., 2015) and uncertainty in modeling assumptions. The impact of end-users' behaviour is surely among the most important factors to be considered (Menezes et al., 2012; Tagliabue et al., 2016). Further, the deployment of new economic (i.e. circular economy) and technological (i.e. Internet of Things) paradigms is routed on the

digitization of equipment and assets, including buildings. The role of people is crucial also in the sense and determines the necessity to address appropriately the incidence of people behavior on energy performance. For this reason it is necessary to identify a reasonable compromise between time and computational effort in modelling and simulation of performance variability determined by people behavior, and to create a "continuity" in the use of models for multiple applications across life cycle phases (i.e. from design to operation).

### Methodology

The increased awareness on sustainability matters is contributing to the evolution of energy and environmental policies for the building sector at the EU level, oriented toward resource efficiency. This evolution is challenging as it claims for an overall coherent, reliable, robust and interoperable model-based approach for performance optimization across building life cycle phases. In fact, while there exist today several possible strategies to model building performance from the energy and environmental standpoint, the relevant gap usually encountered between simulated and measured performance is clearly connected to biased assumptions in modeling, especially in the design phase, and to lack of performance monitoring, in the operation phase. The state of the art of building energy modelling is exhaustively discussed in literature (Zhao and Magoules, 2012; Harish and Kumar, 2016; Fumo, 2014; Fouquier et al., 2014; Coakley et al., 2014; Henze, 2013; Shaikh et al., 2014; Yu et al., 2015). Models used to simulate building energy performance should be aimed at maximizing the value of information, unveiling synergies across multiple processes and scales of analysis. There exists multiple potential feedbacks that can be exploited to improve performance (Fabrizio and Monetti, 2015; Evins, 2013; Nguyen et al., 2014). The first relevant distinction that can be made is among top-down (econometric, technological) and bottom-up (engineering) models (EN 16212, 2012). After that, an important subdivision is related to the different modelling strategies that can be applied in buildings: white-box, grey-box and black-box (Manfren et al., 2013). White-box models are detailed physics-based models, grey-box models are simplified physics-based models and black-box are data driven models based on little or no physical knowledge of the system. The

choice of the modelling approach is determined by the specific objectives and by the required level of detail, accuracy, precision and computational effort. In this research we start from a white-box model and we develop two surrogate models, a grey-box and a black-box one for performance modeling and energy management. The two surrogate modelling approaches selected are respectively a Resistance-Capacitance (RC) model and Artificial Neural Network (ANN), trained on parametric simulation data (Tagliabue et al., 2015). The objective of the research work is assessing the feasibility, reliability and robustness of these two types of surrogate models to compute the energy performance of a case study building in which highly variable occupancy patterns are present, ensuring a more efficient use of the simulation data generated in the design phase. The probabilistic simulation of energy demand is performed by means of Monte Carlo (MC) technique, as indicated in Figure 1.

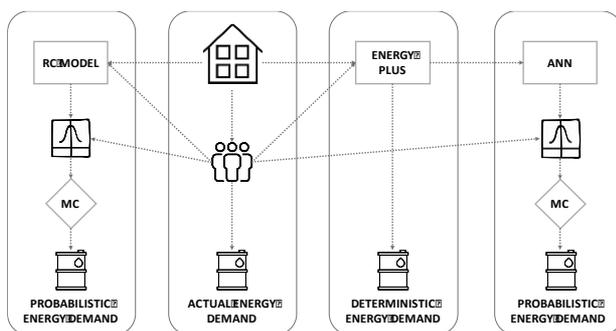


Figure 1: Graphical scheme of research

The overall methodology presented aims at enhancing current practices in performance simulation, highlighting the possibility of using semi-automated/automated approaches to analyze design-phase data, therefore establishing a continuity among design phase tasks (such as design optimization) and operation phase tasks (such as performance monitoring and energy management). The methodology presented is general and an overview of the potential applications using surrogate models in buildings is described in the following section.

## Applications of surrogate models in buildings

The models generally used to simulate building energy behaviour (white-box, physics-based models) present several limitations with respect to automated applications (Hazyuk et al., 2012; Oldewurtel et al., 2012; Privara et al., 2013; Afram and Janabi-Sharifi, 2015). The basic conditions that a model for automated applications should satisfy are reasonable simplicity, enough accuracy in the estimation of system dynamics, usability for prediction in real time operation (Maasoumy and Sangiovanni-Vincentelli, 2012; Hazyuk et al., 2012).

On the one hand, white-box models generally need detailed information and are non-linear problem while linearity (more in general convexity) is an important

feature to obtain easily solvable optimization problems (Oldewurtel et al., 2012; Morari and Lee, 1999; Široký et al., 2011). On the other hand, black-box models, have been widely used in optimal control applications because they can deal efficiently with non-linear problems (Wang S, Jin, 2000). However, they are obtained by means of statistical/machine learning algorithms and, consequently, the identified parameters don't have a physical interpretation, losing a substantial part of the useful information that can be extracted by measured data (Oldewurtel et al., 2012; Afram et al., 2015; Zavala et al., 2011; Zacekova and Privara, 2012; Ferkl and Privara, 2010). In order to overcome these issues, grey-box models, mixing knowledge-based (physics-based) and statistical techniques are used in several applications (Afram and Janabi-Sharifi, 2015; Zacekova and Privara, 2012; Mahdavi, 2001; Jiménez and Madsen, 2008; Bacher and Madsen, 2011). In grey-box modeling the size of the problem is reduced using lumped parameters (Hazyuk et al., 2012; Fouquier et al., 2013; Kramer et al., 2013). The structure of the model (i.e. the reduction strategy) is found by applying basic physical principles (e.g. energy and mass balance) and the parameters can then be estimated both a priori or calibrated on measured data by using identification techniques (Hazyuk et al., 2012; Afram and Janabi-Sharifi, 2015; Hazyuk et al., 2012; European Commission, 2007; Froisy, 2006). The feasibility of integrated and automated performance modeling approaches is confirmed by different international studies on model predictive control (Gwerder et al., 2013) and on building performance characterization based on full-scale dynamic measurement (IEA-EBC). Considering these elements, it is possible to envision a path for the creation of synergies in research field such as design optimization, energy management, diagnostics, and automatic control.

## Case study: the eLUX Lab of Brescia University

The case study presented is the eLUX Lab of the University of Brescia in Italy. The University Campus hosts a multi-disciplinary research initiative focused on Smart technologies (Unibs, 2014; Unibs, 2016). The research, involves multiple topics ranging from BIM (Building Information Modelling) to BEM (Building Energy Modelling), performance optimization, performance monitoring, energy management, user behavioral modeling. In particular, the research on behavioral modeling aims to improve the knowledge of user behavior from a cognitive stand-point, using multiple information sources. In the starting phase of the research activity, prior to refurbishment, a building survey and an energy audit have been conducted. The building has three floors, underground, ground and first floor, with lecture halls and computer labs, and a glazed atrium in which the students can conduct their individual studies, as shown in Figure 2.



Figure 2: External and internal views of the case study building.

The building zones considered for modeling and their net floor surfaces, together with the maximum allowable number of people, are reported respectively in Table 1 and Table 2. The operating schedules of the building are highly variable, due to the different uses of internal spaces.

Table 1: Use of the internal spaces.

Floor	Name	Type of use	Zone
Underground	MLAB1	Computer lab	1
	MLAB2	Computer lab	
Ground	MTA	Classroom	2
	MTB	Classroom	
	Atrium	Common area	3
First	M1	Aula magna	4

Table 2: Size and maximum number of people of the internal spaces.

Floor	Name	Surface	People
		m <sup>2</sup>	n <sub>0,max</sub>
Underground	MLAB1	151.8	56
	MLAB2	207.9	82
Ground	MTA	178.3	168
	MTB	177.5	168
	Atrium	180.8	56
First	M1	337.5	262

**Detailed building energy model**

A detailed (white-box) building energy model has been created in EnergyPlus, starting from building survey and energy audit data. The model has been used initially for the generation of probabilistic energy demand scenarios, considering the use of a Demand Controlled Ventilation (DCV) system, using CO<sub>2</sub> concentration data to control the outdoor fresh airflow rate. In order to generate coherent scenarios, operating schedules and simulation settings have been defined according to the scheme reported in Figure 3 and described in detail in previous research work (Tagliabue et al., 2015). Parametric simulation data obtained from this model have been used to train the ANN model, as explained before.

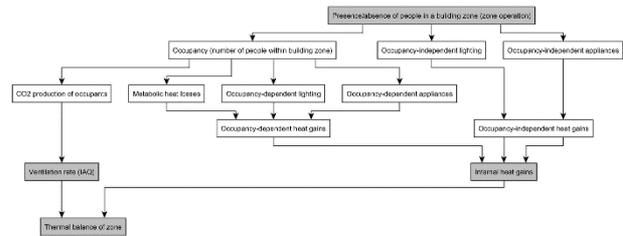


Figure 3: Scheme of the correlation among occupancy schedules and relevant factors affecting thermal balance.

A south-west facing external view of the detailed building energy model is reported in Figure 4.

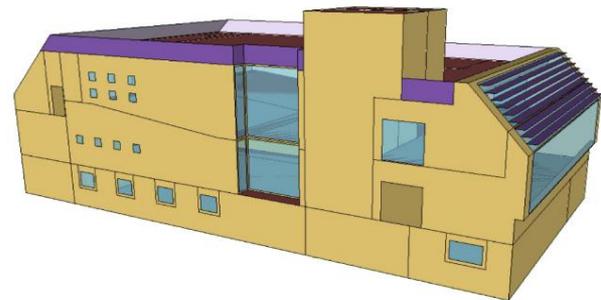


Figure 4: Building energy model in EnergyPlus.

**Resistance-Capacitance (RC) building energy model**

The simplified (grey-box) model is based on Resistance-Capacitance approach (RC), exploiting the electrical analogy for thermal modeling. Therefore, the model is a lumped parameters model for dynamic hourly simulation and optimization.

The building energy model is formulated following the indication given in international standards (UNI EN ISO 13790; UNI EN ISO 13791; UNI EN ISO 13792; UNI EN 15255; 24 ISO 52000). The essential elements of the model are nodes (i.e. temperatures), resistors (i.e. thermal resistances) and capacitors (i.e. thermal capacities). The resistors are necessary to account for heat transfer through construction components and for ventilation. The capacitors are necessary to account for the inertia of construction components. A graphical representation of the model is reported in Figure 5.

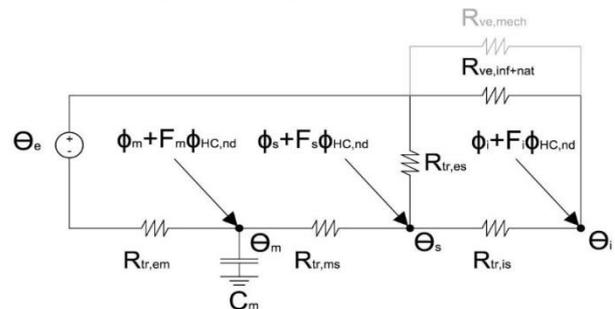


Figure 5: Graphical representation of RC model.

In the graphical representation:

- nodes are:
  - the external air temperature  $\theta_e$ ;
  - the internal air temperature  $\theta_i$ ;
  - the surface temperature  $\theta_s$ ;
  - the mass temperature  $\theta_m$ .
  
- resistances are:
  - the mechanical ventilation  $R_{ve,mech}$ ;
  - the natural ventilation and infiltration  $R_{ve,nat}$ ;
  - the transmission due to no inertia elements  $R_{tr,es}$ ;
  - the transmission due to massive elements  $R_{tr,em}$  and  $R_{tr,ms}$ ;
  - the transmission due to heat exchange between internal air and the internal surface  $R_{tr,is}$ .
  
- capacity is:
  - the global thermal capacity  $C_m$
  
- heat fluxes are:
  - the solar and internal gains fraction on the internal air node  $\Phi_i$
  - the solar and internal gains fraction on the surface node  $\Phi_s$
  - the solar and internal gains fraction on the mass node  $\Phi_m$
  - the heat flow fraction due to heating/cooling system on the internal air node  $F_{i\Phi_{HC,nd}}$
  - the heat flow fraction due to heating/cooling system on the surface node  $F_{s\Phi_{HC,nd}}$
  - the heat flow fraction due to heating/cooling system on the mass node  $F_{m\Phi_{HC,nd}}$

Generally windows elements are considered to have negligible inertia and the related heat transfer coefficient  $H_{tr,es}$  connects directly the external node  $\theta_e$  to the surface node  $\theta_s$ . The heat transmission through the massive elements is divided into three parts, respectively  $H_{tr,em}$ ,  $H_{tr,ms}$  and  $H_{tr,is}$ :

- from the external node  $\theta_e$  to the mass node  $\theta_m$ ;
- from the mass node  $\theta_m$  to the surface node  $\theta_s$ ;
- from the surface node  $\theta_s$  to the internal air node  $\theta_i$ .

The main capacitor of the network represents the lumped global thermal capacity, indicated with  $C_m$ . The total solar  $\Phi_{sol}$  and internal gains  $\Phi_{int}$  are distributed on the internal air node  $\theta_i$ , surfaces node  $\theta_s$  and mass node  $\theta_m$  using coefficients to account for conductive and radiative heat transfer components; the conductive part is assigned to the internal air node  $\theta_i$  while the radiative one to the surface  $\theta_s$  and to the mass  $\theta_m$  nodes. Similarly, the heat flow due to heating and cooling plant  $\Phi_{HC,nd}$  is split into a conductive component, applied to the internal air node  $\theta_i$ , and a radiative component, distributed to the surface  $\theta_s$  and mass nodes  $\theta_m$  according to other factors that are respectively called  $F_i$ ,  $F_s$  and  $F_m$  as suggested by the standards (UNI EN ISO 13792; UNI EN 15255). However, these coefficients can be considered as tunable parameter, within certain limits, for example in a model

calibration process. The simulation with the RC model requires the construction of coherent operating schedules and settings, similarly to the detailed model and differently from the ANN model, which directly learns from data generated by simulation.

### Artificial Neural Network (ANN) model

ANN models for dynamic building performance prediction have already been successfully used in several studies (Paudel et al., 2014; Khayatian et al., 2016). The ANN model used is in this case is a three-layer (input layer-hidden layer-output layer) supervised feedforward network with 59 sigmoid hidden neurons and linear output neurons. The best performing layout has been selected based on the lowest Mean Square Error (MSE) in an automated way. The network used to predict heating demand has a 6 input hourly dataset and 1 output hourly dataset:

- Input 1: outdoor air temperature;
- Input 2: global horizontal solar radiation;
- Input 3-6: occupancy data (i.e. number of users) of the four thermal zones;
- Output 1: thermal energy demand.

The ANN was trained using the Bayesian regularization method and the split of the dataset between training and testing was respectively 75% and 25%. The determination coefficient  $R^2$  obtained by ANN is 0.819 for the training set, 0.812 for the test set, 0.818 for the whole dataset, as reported in Figure 6.  $R^2$  coefficient represents the goodness of fit of the model (maximum value is 1). These values are in line with the ones found in other research studies on dynamic neural network used for heating prediction (Khayatian et al., 2016), which however use additional pseudo dynamic parameter inputs (to improve computing performance and reduce network dimension) that require a priori knowledge of occupancy patterns, while in this case we consider a training process directly on simulation data.

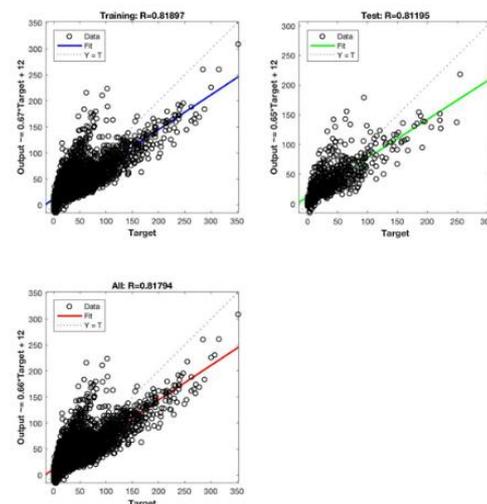


Figure 6: Training and testing of ANN for heating demand prediction

### Monte Carlo simulation of RC and ANN models

Monte Carlo (MC) simulation is one of the most powerful techniques in modern probabilistic analysis. MC methods rely on repeated random sampling to obtain numerical results. By means of MC simulations it is possible to:

1. define a domain of possible model inputs;
2. generate inputs randomly from a probability distribution over the domain;
3. perform a deterministic computation of model outputs;
4. aggregate results and analyze their statistical distribution.

In this research MC simulations have been used to measure how the uncertainty in users' behavior (occupancy patterns) affects heating energy demands calculate by means of RC model and ANN.

Following case studies in literature and previous research work (Tagliabue et al., 2015) we decided to use triangular probability density functions for occupancy. However, differently from to the original simulation work, aimed at exploring highly variable occupancy scenarios, the schedules have been constructed by differentiating the value of the triangular probability distributions in three time intervals, from 9am to 10am, from 11am to 4pm and from 5pm to 7pm. The values assumed in this work are based on the following assumptions:

1. from 9am to 10am:
  - a. minimum value, the corresponding minimum deterministic occupancy pattern;
  - b. mode, the corresponding 1st quartile of deterministic occupancy pattern;
  - c. maximum value, the corresponding maximum deterministic occupancy pattern;
2. from 11am to 4pm:
  - a. minimum value, the corresponding minimum deterministic occupancy pattern;
  - b. mode, the corresponding maximum deterministic occupancy pattern;
  - c. maximum value, the corresponding maximum deterministic occupancy pattern;
3. from 5pm to 7pm:
  - a. minimum value, the corresponding minimum deterministic occupancy pattern;
  - b. mode, the corresponding 3rd quartile of deterministic occupancy pattern;
  - c. maximum value, the corresponding maximum deterministic occupancy pattern.

The results obtained by using MC technique with RC and ANN models are described in the following section.

### Results and discussion

MC simulations have been used to compute a probabilistic distribution of energy demand, using both RC and ANN models, as a function of uncertainty in occupancy patterns. The relation among occupancy patterns and energy balance is described in Figure 3. Both models proved to be suitable in MC simulation because

they are much less computational time than detailed energy simulations and provide reliable results if compared to the ones given by Energy Plus.

Main results are shown in Figure 7 (RC as surrogate model) and in Figure 8 (ANN as surrogate model) where the Cumulative Distribution Function (CDF) of heating demand computed with MC simulations is depicted and compared with a Gaussian distribution having the same mean and standard deviation of MC results.

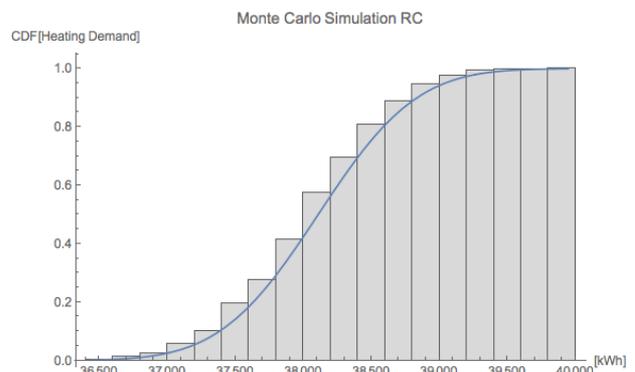


Figure 7: Cumulative Distribution Function of heating demand computed with MC simulation using the RC model compared to a Gaussian with the same mean and standard deviation (blue line).

The small difference in the mean value between the two MC simulations is due to the overestimation of heating energy demand when the demand is small (at the very beginning or at the end of the heating period) made by the ANN. A better tuning of the RC model parameters may also reduce the difference between the two means.

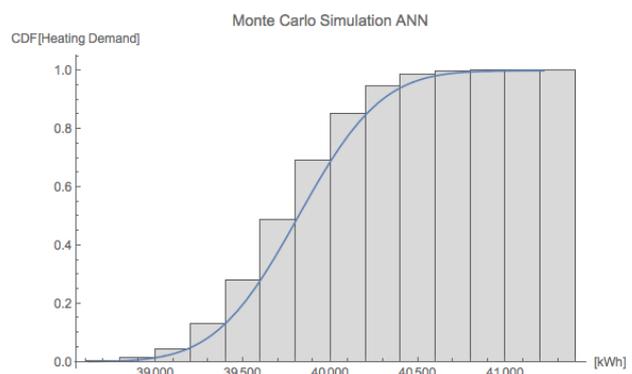


Figure 8: Cumulative Distribution Function of heating demand computed with MC simulation using the ANN model compared to a Gaussian with the same mean and standard deviation (blue line).

The quantiles of the results of MC simulation are reported in Table 3 and compared in Figure 9. This figure highlights the fact that while ANN can be used effectively to reproduce the results of a detailed dynamic model (EnergyPlus) and RC can be used to calculated dynamic

performance producing a similar interval of results, the assumptions on model parameters can produce a misalignments in the data. It is therefore necessary to define strategies to improve the alignment of results computed by the different models, using appropriate data parametrization and metrics (Yang and Becerik-Gerber, 2015).

Table 3: Heating Demand Quantile computed using ANN and RC model

	RC	ANN	RC	ANN
	kWh	kWh	kWh	kWh
<b>5%</b>	37,156	39,221	<b>55%</b>	39,863
<b>15%</b>	37,513	39,435	<b>65%</b>	39,954
<b>25%</b>	37,745	39,568	<b>75%</b>	40,067
<b>35%</b>	37,892	39,673	<b>85%</b>	40,195
<b>45%</b>	38,039	39,766	<b>95%</b>	40,418
<b>50%</b>	38,095	39,813		

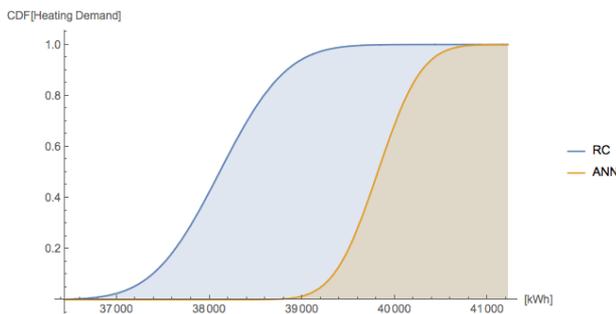


Figure 9: Comparison between heating demand CDF computed with Monte Carlo simulation using RC model and ANN

## Conclusion

The objective of the research work was assessing the feasibility, reliability and robustness of the use of surrogate models to compute energy performance in highly variable conditions. In the research presented, surrogate models have been used to compute efficiently the dynamic energy performance of buildings in presence of highly variable occupancy patterns. These techniques are therefore suitable for the analysis of the impact of end-users' behaviour already from the design phase, identifying probabilistic performance boundaries. The proposed approach aims to ensure a more efficient use of the parametric simulation data generated in the design phase by means of semi-automated/automated modeling tools. Despite the similar ranges of results obtained by the two models, RC and ANN, the research highlighted how further work should be oriented to the definition of appropriate strategies for the alignment of results computed by different models, potentially suitable for multiple applications across building life-cycle phases. These strategies could be based on the definition of macro-parameters and multi-level metrics, as shown in recent research work in the field of model calibration.

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## References

- Afram, A., Janabi-Sharifi, F. (2015) Gray-box modeling and validation of residential HVAC system for control system design. *Applied Energy*. 137:134-50.
- Bacher, P., Madsen, H. (2011) Identifying suitable models for the heat dynamics of buildings. *Energy and Buildings*. 43:1511-22.
- Bynum, J.D., Claridge, D.E., Curtin, J.M. (2012). Development and testing of an Automated Building Commissioning Analysis Tool (ABCAT). *Energy and Buildings*, 55, 607-17.
- Coakley, D., Raftery, P., & Keane, M. (2014). A review of methods to match building energy simulation models to measured data. *Renewable and sustainable energy reviews*, 37, 123-141.
- COM(2011) 112 final. European Commission, A Roadmap for moving to a competitive low carbon economy in 2050.
- De Angelis, E., Re Cecconi, F., Tagliabue, L.C., Maltese, S., Pansa, G., Torricelli, A., Valagussa, S., (2015) Reliability of energy performance evaluations through different BIM to BEM models, *Sostenibilità Ambientale e Produzione*, Edilizia Maggioli Editore.
- De Wilde, P. (2014). The gap between predicted and measured energy performance of buildings: A framework for investigation. *Automation in Construction*, 41, 40-49.
- Evins, R. (2013). A review of computational optimisation methods applied to sustainable building design. *Renewable and Sustainable Energy Reviews*, 22, 230-245.
- EN 16212:2012, Energy Efficiency and Saving Calculation – Top-down and Bottom-up Methods.
- EnergyPlusTM (2013) Getting Started with EnergyPlus: Basic Concepts Manual – Essential Information You Need about Running EnergyPlus (and a start at building simulation)”, The Board of Trustees of the University of Illinois and the Regents of the University of California through the Ernest Orlando Lawrence Berkeley National Laboratory (LBNL, California).
- European Commission, Programme IEE (Intelligent Energy Europe), Building EQ - The EPBD and Continuous Commissioning - Tools and methods for linking EPBD and continuous commissioning. 2007.

- Fabrizio, E., & Monetti, V. (2015). Methodologies and advancements in the calibration of building energy models. *Energies*, 8(4), 2548-2574.
- Ferkl, L., Privara S. (2010) Model predictive control of buildings: The efficient way of heating. Control Applications (CCA), 2010 IEEE International Conference on. Yokohama, Japan. p. 1922-6.
- Fouquier, A., Robert, S., Suard, F., Stéphan, L., & Jay, A. (2013). State of the art in building modelling and energy performances prediction: A review. *Renewable and Sustainable Energy Reviews*, 23, 272-288.
- Fouquier, A., Brun, A., Faggianelli, G.A., Suard, F. (2013) Effect of wall merging on a simplified building energy model: accuracy vs number equations. 13thConf Intl Building Perf Simulation Ass. Chambéry, France.
- Froisy, J.B. (2006) Model predictive control—Building a bridge between theory and practice. *Computers & Chemical Engineering*, 30:1426-35.
- Fumo, N. (2014). A review on the basics of building energy estimation. *Renewable and Sustainable Energy Reviews*, 31, 53-60.
- Gwerder, M., Tödtli, J. (2005) Predictive control for integrated room automation. 8th REHVA World Congress Clima. Lausanne, Switzerland.
- Gwerder, M., Gyalistras, D., Sagerschnig, C., Smith, R.S., Sturzenegger, D., (2013) Final Report: Use of weather and occupancy forecast for optimal building climate control (Opticontrol), Automatic Control Laboratory, ETH Zurich, Switzerland.
- Khayatian, F., Sarto, L., Dall'O', G., (2016) Application of neural networks for evaluating energy performance certificates of residential buildings, *Energy and Buildings*, 125, 45–54.
- Kramer, R., van Schijndel, J., Schellen, H. (2013) Inverse modeling of simplified hygrothermal building models to predict and characterize indoor climates. *Building and Environment*.;68:87-99.
- Harish, V. S. K. V., & Kumar, A. (2016). A review on modeling and simulation of building energy systems. *Renewable and Sustainable Energy Reviews*, 56, 1272-1292.
- Hazyuk, I., Ghiaus, C., Penhouet, D. (2012) Optimal temperature control of intermittently heated buildings using Model Predictive Control: Part II – Control algorithm. *Building and Environment*. 51:388-94.
- Hazyuk, I., Ghiaus, C, Penhouet, D. (2012) Optimal temperature control of intermittently heated buildings using Model Predictive Control: Part I – Building modeling. *Building and Environment*. 51:379-87.
- Henze, G. P. (2013). Model predictive control for buildings: a quantum leap?. *Journal of Building Performance Simulation*, 6(3), 157-158.
- International Energy Agency (IEA - EBC), Annex 58: Reliable Building Energy Performance Characterization based on full scale dynamic measurement.
- ISO 52000:2014, Energy performance of buildings - Overarching EPB assessment.
- Jiménez, M.J., Madsen, H. (2008) Models for describing the thermal characteristics of building components. *Building and Environment*. 43:152-62.
- Maasoumy, M., Sangiovanni-Vincentelli, A. (2012) Total and peak energy consumption minimization of building hvac systems using model predictive control. *IEEE Design & Test of Computers*. 29.
- Mahdavi, A. (2001) Simulation-based control of building systems operation. *Building and Environment*. 36:789-96.
- Manfren M., Aste N., Moshksar R. (2013) Calibration and uncertainty analysis for computer models – A meta-model based approach for integrated building energy simulation. *Applied Energy*. 103:627-641.
- Menezes A.C., Cripps A., Bouchlaghem D., Buswell R., (2012) Predicted vs. actual energy performance of non-domestic buildings: Using post-occupancy evaluation data to reduce the performance gap. *Applied Energy*. 97:355-364.
- Morari M, H. Lee J. (1999) Model predictive control: past, present and future. *Computers & Chemical Engineering*. 23:667-82.
- Nguyen, A. T., Reiter, S., & Rigo, P. (2014). A review on simulation-based optimization methods applied to building performance analysis. *Applied Energy*, 113, 1043-1058.
- Oldewurtel, F., Parisio, A., Jones, C.N., Gyalistras, D., Gwerder, M., Stauch, V., et al. (2012) Use of model predictive control and weather forecasts for energy efficient building climate control. *Energy and Buildings*. 45:15-27.
- Paudel S., Elmtiri M., Kling W.L., Corre O.L., Lacarrière B., (2014) Pseudo dynamic transitional modeling of building heating energy demand using artificial neural network, *Energy and Buildings*, 70, 81-93
- Privara, S., Cigler, J., Vána, Z., Oldewurtel, F., Sagerschnig C, Žáčková E. Building modeling as a crucial part for building predictive control. *Energy and Buildings*. 2013;56:8-22.
- Shaikh, P. H., Nor, N. B. M., Nallagownden, P., Elamvazuthi, I., & Ibrahim, T. (2014). A review on optimized control systems for building energy and comfort management of smart sustainable buildings. *Renewable and Sustainable Energy Reviews*, 34, 409-429.

- Široký J, Oldewurtel F, Cigler J, Prívvara S. (2011) Experimental analysis of model predictive control for an energy efficient building heating system. *Applied Energy*. 88:3079-87.
- Tagliabue, L.C., Manfren, M., Ciribini, A., De Angelis, E., (2016), Probabilistic behavioural modeling in building performance simulation—The Brescia eLUX lab, *Energy and Buildings*, 128, 119-131.
- Tagliabue, L.C., Manfren M., Enrico De Angelis, Angelo Luigi Camillo Ciribini, Energy Efficiency Assessment Based on Realistic Occupancy Patterns Obtained through Stochastic Simulation, in Modelling Behaviour: Design Modelling Symposium 2015, a cura di Mette Ramsgaard Thomsen, Martin Tamke, Christoph Gengnagel, Billie Faircloth, Fabian Scheurer, Springer, 2015, Pag. 469-478, ISBN 978-3-319-24206-4.
- Tronchin, L., Manfren, M., Tagliabue L.C. (2015). Multi-scale analysis and optimization of building energy performance—Lessons learned from case studies. *Sustainable Cities and Society*, 118:563–572.
- UNI EN ISO 13790:2008, Energy performance of buildings, Calculation of energy use for space heating and cooling.
- UNI EN ISO 13791:2012 Thermal performance of buildings - Calculation of internal temperatures of a room in summer without mechanical cooling - General criteria and validation procedures.
- UNI EN ISO 13792:2012 Thermal performance of buildings Calculation of internal temperatures of a room in summer without mechanical cooling - Simplified methods.
- UNI EN 15255:2008, Energy performance of buildings - Sensible room cooling load calculation - General criteria and validation procedures.
- University of Brescia (2014-2016) Regione Lombardia under Smart cities and communities grant no. 40545387 “Smart Campus as Urban Open Labs – SCUOLA”, <http://es3.unibs.it/SCUOLA/>
- University of Brescia (2016) “Energy Laboratory as Univesrity Expo – eLUX”, <http://elux.unibs.it/>
- Wang S, Jin X. (2000) Model-based optimal control of VAV air-conditioning system using genetic algorithm. *Building and Environment*.;35:471-87.
- Yang Z., Becerik-Gerber B. (2015) A model calibration framework for simultaneous multi-level building energy simulation. *Applied Energy*, 149:415-431
- Yu, Z. J., Huang, G., Haghghat, F., Li, H., & Zhang, G. (2015) Control strategies for integration of thermal energy storage into buildings: State-of-the-art review. *Energy and Buildings*, 106, 203-215.
- Zacekova, E., Privara, S. (2012) Control relevant identification and predictive control of a building. Control and Decision Conference (CCDC), 24th Chinese. Taiyuan, China. p. 246-51.
- Zavala, V.M. (2012) Real-Time Optimization Strategies for Building Systems. *Industrial & Engineering Chemistry Research*. 52:3137-50.
- Zavala V, Skow D, Celinski T, Dickinson P. Techno-economic evaluation of a next-generation building energy management system. Technical Report ANL/MCS-TM-313, Argonne National Laboratory; 2011.
- Zhao, H. X., & Magoulès, F. (2012). A review on the prediction of building energy consumption. *Renewable and Sustainable Energy Reviews*, 16(6), 3586-3592.